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Gas-Flow Sensor Based on Self-Oscillating and Self-Sensing Cantilever [†]

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Abstract: In this work the application of a self-sensing and self-actuating cantilever for gas-flow measurement is investigated. The cantilever placed in the flow is excited permanently at its first resonance mode. Simultaneously the resonance amplitude, the resonance frequency and the static bending of the cantilever are detected. All three sizes are related to the velocity of the gas-flow.

Keywords: gas-flow sensor; cantilever; piezo-resistive sensing; PLL; resonance mode

1. Introduction

Flow sensors are widely used in industry, laboratories, medicine and home. Frequently used mass flow measurement principles are based on thermal conductivity of the gas, float-style, Coriolis force, vortex shedding and differential pressure. Flow sensors based on micro-cantilevers have already been presented in literature [1,2] where a cantilever projecting into a flow stream bends or is vibrated by the flow.

Micro- and nano-cantilevers used among as probes in atomic force microscopy are capable to detect smallest forces [3]. In this patent pending work, these highly sensitive cantilevers with integrated actuator und piezo-resistive read-out were used to measure the gas-flow. This cantilever type allows the flow to be measured simultaneously in two ways with a single sensor. The cantilever is placed in a flow channel, perpendicular to the flow direction and is excited in resonance vibration. Firstly, the cantilever is bent by the flow forces (here called - static operating mode) and secondly its resonance behavior is changed (dynamic operating mode). In the static operating mode, the bending is proportional to the square of the gas-flow velocity. In dynamic operating mode, the resonance amplitude is attenuated with increasing flow velocity and the resonance frequency is slightly shifted to higher values.

2. Experimental Setup and Behavior Description

For the investigations, cantilevers with rectangular cross-section (length $l = 350 \mu\text{m}$, width $w = 140 \mu\text{m}$ and thickness $d = 5 \mu\text{m}$) are used (Figure 1). The cantilever has a thermo-mechanical actuator. It is based on a two-layer structure with different thermal expansion coefficients, the silicon beam and an aluminum meander. The aluminum meander also serves as a heating resistor. The emitted heat

changes the temperature of the cantilever and its bending. A periodic heating voltage causes the cantilever to oscillate. At the clamping point of the cantilever a Wheatstone bridge of four piezo-resistors is positioned. It serves to detect the deflection of the cantilever.

The cantilever is placed perpendicular to the gas-flow direction in a circular channel. By means of commercial mass flow controllers defined flow rates of different gases (in this work: air and CO₂) are set. The dynamic excitation of the cantilever takes place via a DDS (direct digital synthesis) generator and the resulting cantilever oscillation is detected frequency sensitive with a lock-in amplifier. Because of the resonance frequency shift due to the gas-flow, a PLL (phase locked loop) was used to ensure that the cantilever permanently oscillates at the resonance point. Resonance amplitude and resonance frequency are detected. Parallel to this, the static deflection of the cantilever is measured.

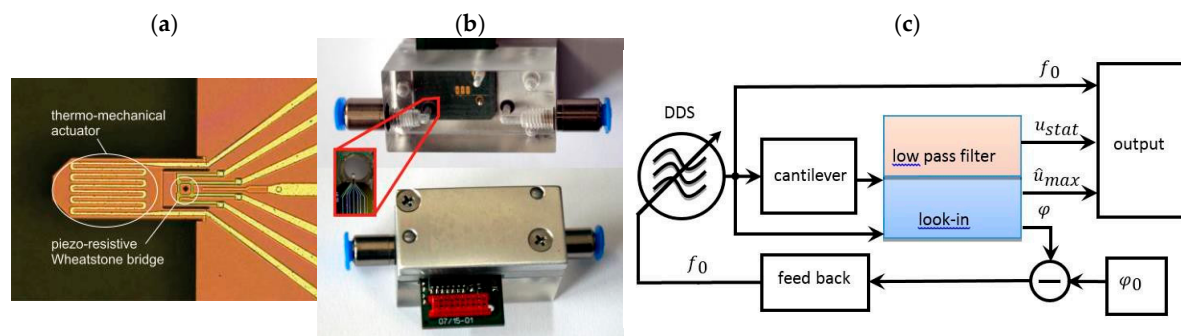


Figure 1. (a) Self-actuated cantilever with integrated read-out; (b) gas-flow sensor enclosure with cantilever and preamplifier; (c) diagram of PLL based sensor control with signal separation.

The cantilever behavior with respect to external force can be described by the differential equation of the simple harmonic oscillator:

$$m_{eff} \cdot \frac{d^2x}{dt^2} + D \cdot \frac{dx}{dt} + k \cdot x = F(t) \quad (1)$$

with m_{eff} —the effective mass, x —the deflection, t —the time, D —the damping, k —the spring constant and F —the external forces. In the case of a periodic force the oscillation amplitude is defined as

$$\hat{x}(\omega) = \frac{\hat{F}/m_{eff}}{\sqrt{(\omega_0^2 - \omega^2)^2 + \left(\frac{D}{m_{eff}}\omega\right)^2}} \quad (2)$$

with $\omega_0 = 2\pi f_0 = \sqrt{\frac{k}{m_{eff}}}$ —resonance frequency and ω —the excitation frequency. The resonance amplitude is significantly dependent on the damping:

$$\hat{x}_{max} = \frac{\hat{F}/m_{eff}}{\omega_0^2} \cdot \frac{\omega_0}{D/m_{eff}} \cdot \frac{1}{\sqrt{1 - \left(\frac{D/m_{eff}}{2\omega_0}\right)^2}} \approx \frac{\hat{F}/m_{eff}}{\omega_0^2} \cdot \frac{\omega_0}{D/m_{eff}} \approx \frac{\hat{F}/m_{eff}}{\omega_0^2} \cdot Q \quad (3)$$

In this manner we can determine the quality factor Q at the resonance of the cantilever. Under the action of a constant force, Hooke's law follows:

$$k \cdot x = F \quad (4)$$

In addition, for the description of the movement of the cantilever in a gas atmosphere under normal pressure (1013 mbar), it is assumed that the gas can be regarded as a viscous liquid.

First, we are considering a non-oscillating cantilever placed in the gas stream. It is deflected by the drag force. The cantilever deflection x_0 depends on the velocity v_0 according to

$$k \cdot x_0 = F_D = \frac{1}{2} \cdot \rho_{gas} \cdot w \cdot l \cdot C_D \cdot |v_0| \cdot v_0 \quad (5)$$

The drag coefficient C_D depends on the geometry of the body and the flow conditions, quantified by the Reynolds number

$$Re = \frac{\rho_{gas} \cdot w \cdot v_0}{\eta_{gas}} \quad (6)$$

with ρ_{gas} —the gas density, η_{gas} —the dynamic viscosity of the gas and w —the cantilever width. For the output signal of the sensor (voltage of the Wheatstone bridge) follows

$$u_{stat} \sim x_0 \sim v_0^2. \quad (7)$$

It should be noted that for low Reynolds numbers, i.e., for small flow velocities the drag coefficient changes relatively strongly with the flow velocity, which consequently means a deviation from the quadratic dependence in this range.

Now, if the cantilever is excited at resonance, the movement of the cantilever overlaps with the gas-flow. For the force acting on a resonating cantilever ($\omega_{0,gas}$ —the resonance frequency in gas) follows

$$F_D = \frac{1}{2} \cdot \rho_{gas} \cdot w \cdot l \cdot C_D \cdot |v_0 - \hat{x} \cdot \omega_0 \cdot \sin(\omega_{0,gas}t)| \cdot (v_0 - \hat{x} \cdot \omega_{0,gas} \cdot \sin(\omega_{0,gas}t)). \quad (8)$$

Assuming that the cantilever velocity is small compared to the flow velocity (this is true for a wide range of applications: $v_0 = 0,5..30m/s$, $\hat{x} \cdot \omega_{0,gas} \approx 0,05m/s$), one obtains

$$\begin{aligned} F_D &\approx \frac{1}{2} \rho_{gas} w l C_D |v_0| v_0 - \rho_{gas} w l C_D |v_0| \hat{x} \omega_{0,gas} \sin(\omega_{0,gas}t) \\ &\approx \frac{1}{2} \rho_{gas} w l C_D |v_0| v_0 - D_v \hat{x} \omega_{0,gas} \sin(\omega_{0,gas}t). \end{aligned} \quad (9)$$

The 1st term describes the flow force that causes the static bending of the cantilever (see Equation (5)), and the second term the force that counteracts the vibration movement, i.e., that damps the oscillation.

This damping increases with increasing flow velocity

$$D_v = \rho_{gas} w l C_D |v_0| \quad (10)$$

and leads to a decrease in the oscillation amplitude. The amplitude of the periodic part of the sensor signal shows the following relationship

$$\hat{u}_{max} \sim \hat{x}_{max} \sim \frac{1}{D_v} \sim \frac{1}{|v_0|}. \quad (11)$$

Since the damping of the oscillation of a cantilever does not disappear in the quiescent gas, this proportion must be taken into account. It was examined for a quiescent fluid in [4–6]. The following relationship for viscous damping was given by Maali et al. [6]:

$$\begin{aligned} D_0 &\approx \frac{\pi}{4} \cdot \rho_{gas} \cdot w^2 \cdot l \cdot \omega_{0,gas} \cdot \left\{ 3,8018 \cdot \frac{\delta}{w} + 2,7364 \cdot \left(\frac{\delta}{w} \right)^2 \right\} \\ &= \frac{\pi}{2} \cdot \eta_{gas} \cdot l \cdot \left\{ 3,8018 \cdot \frac{w}{\delta} + 2,7364 \right\} \end{aligned} \quad (12)$$

the cantilever, l —the length of the cantilever, ρ_{gas} - the density of the gas and η_{gas} the dynamic viscosity of the gas. The 1st term describes the influence of movement of the cantilever on the damping, it increases with decreasing viscous layer thickness δ , which gets smaller with rising frequency $\omega_{0,gas}$, and the second term is the so-called Stokes' term. This means that the damping of the oscillating cantilever is determined by Equation (12) for small flow velocities and satisfies the dependence of (10) for larger velocities. A simple approach is to add both parts together

$$D = D_0 + D_v \quad (13)$$

Furthermore, according to [6], the amount of gas co-moved by the oscillating cantilever causes a reduction of the resonance frequency in respect to the resonance frequency in vacuum

$$\frac{\omega_{0,vac}}{\omega_{0,gas}} \approx \sqrt{1 + \frac{\rho_{gas} \cdot \pi \cdot w}{4 \cdot \rho \cdot d} \cdot \left[1,0553 + 3,7997 \frac{\delta}{w} \right]}. \quad (14)$$

At higher resonance frequencies, a small decrease in this influence occurs due to the thickness reduction of the viscous boundary layer δ . The gas-flow also influences this boundary layer around the cantilever.

3. Results

The responds of the cantilever sensor in respect to the gas-flow through a channel with a diameter of 1 mm is shown in Figure 2 for air and CO₂. All 3 measured variables - the resonance amplitude, the resonance frequency and the static deflection – are changed due to the gas-flow:

- The static deflection increases quadratically with the flow velocity according to equation (5). In the lower flow range, the measurement is inaccurate due to the very small responds and the noise of the static measurement.
- The resonance amplitude drops with $1/v$. It has a high sensitivity in the flow range of 1–10 m/s. In this range it decreases by 50%.
- The resonance frequency increases linearly with the flow velocity. The change is small: $\frac{\Delta f_0/f_0}{\Delta v_0} \approx 0,1 \dots 0,2 \% / \frac{m}{s}$. The size of the resonance frequency and its change as a function of the gas-flow is gas type dependent.

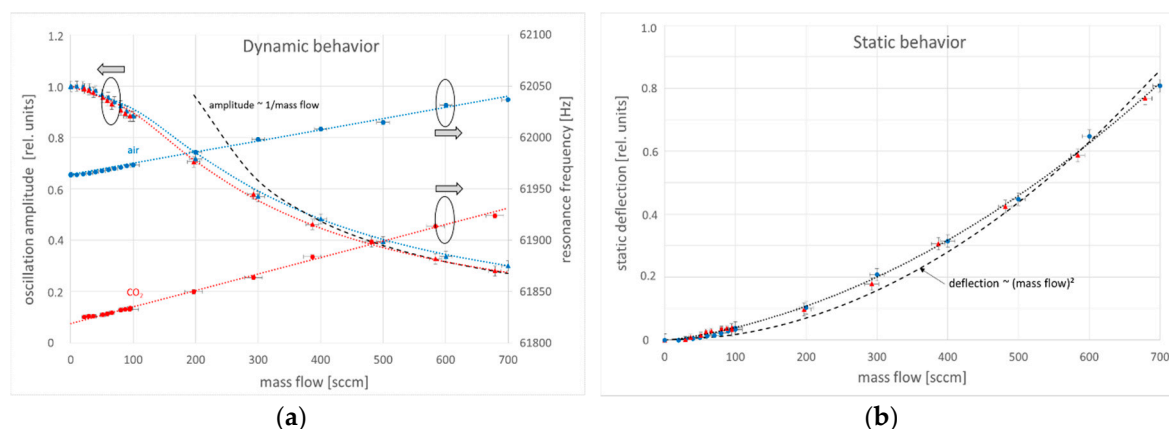


Figure 2. (a) Measured dependency of resonance amplitude, resonance frequency and (b) bending of the cantilever sensor on the gas-flow through a tube with 1 mm diameter (dotted line—fitted curve, dashed line—simplified behavior, symbols - measured values, blue—air, red—CO₂).

A combination of both methods offers an extension of the measuring range and accuracy, as well the gas type determination.

Author Contributions: J.-P.Z., I.W.R. and S.D. conceived and designed the experiments; J.-P.Z., J.S. and S.D. performed the experiments and analyzed the data; T.I. and M.H. designed and fabricated the cantilever; W.E. developed the electronic; W.U.R. constructed and built the sensor enclosure; J.-P.Z. wrote the paper.

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Conflicts of Interest: The authors declare no conflict of interests.

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